When Is Building a Library Consortium Beneficial?*

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Abstract

Electronic publishing has induced libraries to form a consortium, whereby libraries join forces to share acquisition of electronic academic journals. Building a consortium offers both opportunities and pitfalls and this paper identifies strategies to build a library consortium from a long term point of view. Contrary to the conventional wisdom to build a consortium around groups of homogenous institutions (Davis, 2002), we find that libraries with similar preferences are likely to lose from building a consortium while libraries with opposite preferences almost always gain from it. Our results point out a tension between a short-term strategy and a long-term strategy as long as the former dictates forming a consortium around libraries with homogenous preferences in order to gain from quantity discounts. To the contrary, libraries should aim at building a level-playing field among powerful publishers by forming a consortium with libraries having opposite preferences.

Keywords: Library Consortium, Academic Journals, Personalized Prices, Correlation, Multimarket contact, Level-playing Field

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1 Introduction

Electronic publishing has brought fundamental changes in the market for academic journals. It allowed large publishers to practice ‘Big Deal’\(^1\) pricing strategies by bundling a large collection of journals. At the same time, it induced libraries to form consortia, whereby libraries of a given geographical area join forces in order to share acquisition of electronic academic journals licensed through the Big Deal.

Academic library consortia are widespread. Virtually every country or region has built or has the possibility of building a national or regional library consortium. North American examples include OhioLINK, the Triangle Research Libraries Network of North Carolina (TRLN), the Greater Western Library Alliance (GWLA), the Colorado Alliance of Research Libraries (CARL) and the Ontario Council of University Libraries (OCUL). Some well-known European groups include HEAL-LINK (Greek academic libraries including the National Library) and CBUC (academic libraries of Catalonia in Spain).\(^2\) Moreover, existing consortia can decide to expand by forming a mega consortium.

In this paper, we study the conditions that make a library consortium beneficial. In other words, we attempt to study strategies to make a library consortium successful from a long-term perspective as is suggested by Thomas A. Peters (2001a), director of center for library initiatives,

“One challenge for academic library consortia is to shift gears and engage in more deliberate strategic planning with an eye to positive long-terms outcomes”.

If one thinks that publishers propose menu of prices with quantity discounts based on the number of potential users, then it might be desirable to build consortia with libraries with similar preferences in terms of their preferred journals. Actually, this strategy is what Philip M. Davis (2002), a bibliographer at Cornell University, recommends.

“It is recommended that institutions consider their consortia membership and organize themselves into groups of homogenous institutions with similar missions”.

However, the reasoning based on quantity discounts implicitly assumes that publishers’ price schedules do not change much after forming a consortium, which can be true in a short-run but cannot be true in a long-run. In fact, Dewatripont et al. (2006) point out

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\(^1\)Big Deal is defined as “any online aggregation of e-content that a publisher, aggregator, or vendor offers for sale or lease at prices and/or terms that substantially encourage acquisition of the entire corpus” (Peters, 2001b).

\(^2\)Other examples include: CAUL CEIRC (Australia), ANSF (Brazil), CALIS (China), MALKAD (Israel), INFER (Italy).
that “we may fear that consortia in fact strengthen the possibility for publishers to charge a high price for their electronic collection (p.52).”

In this paper, we take a long-term view in the sense that publishers change their prices after libraries form a consortium. Actually, publishers’ price offers are tailored directly to individual characteristics of libraries or consortia. Furthermore, it is now easy to estimate the value of a given journal to a library since its publisher and the library can observe the number of downloads of the journal (Gatten and Sanville, 2004 and Scigliano 2010).

In our framework, each (for-profit) publisher competes by offering its bundle of journals at a personalized price to each different library (or consortium) under complete information about the library’s preferences and budget (Jeon and Menicucci, 2006 and 2011). When several libraries build a consortium, we assume that all their budgets are pooled and the consortium maximizes the sum of each member library’s surplus. However, building the consortium triggers publishers’ reactions since each publisher now offers a new personalized price of its bundle to the consortium, taking into account the preferences and budget of the consortium. In this framework, we study the conditions under which building a consortium is beneficial.

Since we consider that publishers make price offers (simultaneously) before libraries make purchase decisions, our model does not capture any gain from increase in the buyer power of libraries. However, Dewatripont et al. (2006) argue that "since researchers do not see the various publishers as good substitutes and need access to all journals, consortia only introduce a relatively weak ‘buyer power’ (p.8)." In addition, in our framework, there is no gain from building a consortium in the case of a monopolist publisher since a monopolist charges a price equal to the budget (as long as the value of the bundle of the monopolist is not smaller than the budget, which we assume).

Therefore, we essentially focus on how a consortium affects the competition among publishers, which we think provides a long-term perspective since only competition can restrain the amount of surplus that each publisher can extract in a long run. More precisely, we focus on the question of whether a consortium should be formed by libraries with similar preferences (as Davis (2002) recommends) or by libraries with opposite preferences.

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3 According to Edlin and Rubinfeld (2004), “Here, the price that a buyer is quoted depends upon the buyer’s observable characteristics. ... Moreover, in practice, the price of the Big Deal is often individually negotiated with a given library or with groups of libraries called “consortia,” offering further opportunities for the publisher to price based on individual characteristics.”

4 According to Derk Haank (2001), CEO of Elsevier Science “What we are basically doing is to say that you pay depending on how useful the publication is for you - estimated by how often you use it.”

5 Dewatripont et al. (2006) also write, “This ‘buyer concentration’ remains however modest in comparison with publisher concentration: the largest library consortium represents 2 or 3% of global journal purchases, while the largest publisher represents more than 20% of journal sales (p.8)”.

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In fact, Gatten and Sanville (2004) compute the Spearman’s correlation coefficients between each pair of member institutions of OhioLINK, which varies between -1 and 1\(^6\) and find that overall relative use of Big Deal titles between member institutions correlates highly. Hence, correlation among libraries’s preferences is a key dimension for consortium strategy.

Contrary to some conventional wisdom to build consortium around groups of homogeneous institutions (Davis, 2002), we find that (i) libraries with similar preferences have almost nothing to gain or lose from building a consortium; (ii) libraries with opposite preferences almost always gain from building a consortium; (iii) in general, building a consortium increases the total surplus only if the member libraries’ preferences are heterogeneous enough to create a level-playing field among different individually-preferred publishers.

In our model, each publisher sells a bundle of all its journals. This pure bundling strategy captures the "Big Deal" practice and there is no loss of generality in restricting each publisher to use the pure bundling strategy (see footnote 9). In addition, the value that a library obtains from a bundle of journals is assumed to be independent from the value that it obtains from another bundle. Therefore, competition among bundles of journals in the market for a given library is generated by the library’s budget constraint. In particular, if the library prefers too much the bundle of a certain publisher, this can induce a monopoly outcome in the sense that there is no budget left for other bundles after paying for the preferred bundle.

In order to provide an intuition for our results, let us first consider the case of two identical libraries (i.e. the extreme case of perfectly positive correlation). Then, the consortium has no impact neither on libraries nor on publishers, since each library continues to consume the same bundles and bear the same expenses, as without the consortium. Consider now the other extreme case of perfectly negative correlation. Suppose that library 1 (2) likes so much bundle A (B) that library 1 (2) consumes only bundle A (B) in the absence of the consortium. Then, building a consortium creates a level-playing field between the two publishers such that no publisher monopolizes the market for the consortium and each library ends up consuming both bundles. Last, let us consider the intermediate case in which library 1 consumes only bundle A while library 2 consumes both bundles A and B without the consortium. Then, the consortium can either increase or decrease the total surplus depending on the size of its budget. If the budget is small enough, publisher A can export its residual monopoly power from library 1 to library 2 and monopolize the entire market of the consortium. On the contrary, if the budget is large enough, publisher A cannot monopolize the entire market of the consortium and the

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\(^6\)For this, they first compute the rank order of titles by each institution’s total downloads and study how closely the rank orders of each pair of institutions correlate.
consortium consumes both bundles. This logic is similar to that of multimarket contact in collusion (Bernheim and Whinston, 1990).

We show that our main insight is robust to making the budget of each library endogenous. Actually, the prediction becomes sharper in the case of endogenous budget since two libraries can never gain from building a consortium when their preferences are positively correlated no matter what the degree of correlation. We find that in this case, by building a consortium, the funding authority loses instruments to implement library-specific consumption patterns while it can achieve the consumption pattern of consortium at the same total price without consortium. In the case of negative correlation, the result obtained from the scenario of endogenous budget is remarkably similar to the result obtained from the scenario of exogenous budget: in both scenarios, the range of parameters for which building a consortium is beneficial increases with the absolute degree of correlation.

Our paper builds on the literature on the market for academic journals which studies issues raised by the move to electronic publishing.\(^7\) The literature has studied bundling and/or price discrimination (McCabe, 2004, Jeon and Menicucci, 2006, Armstrong 2010), interoperability (Jeon and Menicucci, 2011), open access journals (McCabe and Snyder, 2007, Jeon and Rochet, 2010). We contribute to the literature by studying the issue of library consortium.

Our main contribution with respect to the literature on buyer coalition is that we consider competing sellers whereas the literature considers the monopoly setting. For instance, Innes and Sexton (1993, 1994) analyze the case in which a monopolist is facing identical consumers who may form coalitions. They show that even though consumers’ characteristics are homogeneous, the monopolist may price discriminate in order to deter the formation of coalitions, whereas price discrimination is unprofitable in the absence of coalitions. Alger (1999) studies a monopolist’s optimal menu of price-quantity pairs when (a continuum of) consumers can purchase multiple times and/or jointly in a two-type setting. While the previous papers consider coalition formation under complete information, Jeon and Menicucci (2005) study a monopolist’s optimal menu of price-quantity pairs when buyers form a coalition under asymmetric information between themselves.

Our result that buyers with opposite preferences (instead of buyers with similar preferences) should form a consortium is reminiscent of a classic paper in the bundling literature, Adams and Yellen (1976), that shows that pure bundling of two products gives a monopolist a higher (resp. a lower) profit than independent pricing if buyers’ valuations of the products are negatively correlated (resp. positively correlated). However, the two papers differ in many aspects. Adams and Yellen consider bundling of two products sold by a monopolist to a mass of heterogenous consumers whereas we study library consortium when publishers compete by offering personalized prices to each buyer.

\(^7\)See Bergstrom (2001) and Dewatripont et al. (2006) for an introduction.
Although we consider a common agency under complete information, (Bernheim and Whinston, 1986, 1998, Jeon and Menicucci, 2012), the well-known result that the competition among the sellers achieves the outcome that maximizes the joint payoff of all sellers and the buyer fails to hold in our setting because of the budget constraint.\(^8\)

Our paper also belongs to the emerging literature on personalized pricing (Chen and Iyer, 2002, Choudhary et al., 2005, Ghose and Huand, 2009, Shaffer and Zheng, 2002, Thisse and Vives, 1988). Personalized pricing refers to the practice that firms offer customized prices on a one-to-one basis to each customer (an individual or a firm), which has become possible since advances in information technologies and the Internet allow firms to identify each customer with greater accuracy and cost-effectiveness. The papers mentioned above model personalized pricing as perfect price discrimination as in our paper.

The paper is organized as follows. Section 2 presents our model. Section 3 obtains a general result in the case of a consortium of \(n\) libraries. Section 4 provides more precise results focusing on correlation of preferences by considering a consortium of two libraries. Section 5 studies the scenario of endogenous budget. Section 6 derives policy implications from our results.

## 2 Model

As we mentioned in the introduction, we take the model of our previous papers (Jeon and Menicucci, 2006 and 2011) and assume that publishers have complete information about the value that a library attaches to each journal and about the library’s budget, and offer personalized prices based on the information. In the baseline model, the budget of each library is exogenously given. In Section 5, we study the scenario in which the budget of each library is endogenously determined.

### 2.1 Publishers, libraries, and consortium

There are two (for-profit) publishers, \(A\) and \(B\), and \(n \geq 2\) libraries. Without loss of generality, we assume that each publisher offers only the pure bundle of its own journals.\(^9\) Let \(B_j\) represent the bundle offered by publisher \(j\) (= \(A, B\)). The monetary utility of library \(i\) (= \(1, \ldots, n\)) from consuming \(B_j\) is denoted by \(U^j_i > 0\), and the budget of library \(i\) is \(M^i > 0\). The payoff of a library is given by the utility it obtains from the bundles of

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\(^8\)On the contrary, Jeon and Menicucci (2012) find that the result holds when the buyer has a slot constraint instead of the budget constraint.

\(^9\)Arguing as in the proof of Proposition 2(i) in Jeon and Menicucci (2006), we can prove that, for each publisher, pure bundling of its journals weakly dominates any alternative to pure bundling.
journals it buys minus the money it spends for the purchases.

Let \( C \) represent the consortium of the \( n \) libraries. The utility of the consortium \( C \) from consuming \( B_j \) and the budget of the consortium are given by:

\[
U^C_j = \sum_{i=1}^{n} U^i_j, \quad M^C = \sum_{i=1}^{n} M^i.
\]

As for each member library, the payoff of the consortium is the utility it obtains from the bundles of journals it buys minus the money it spends for the purchases.

Let \( P^i_j > 0 \) represent the price that publisher \( j (= A, B) \) charges to library \( i (= 1, \ldots, n, C) \) for bundle \( B_j \). We assume that the fixed cost of producing the first copy of each journal in \( B_j \) has already been incurred and that the marginal cost of distributing a journal is zero. Therefore, publisher \( j \)'s profit is equal to publisher \( j \)'s revenue.

Social welfare is defined as the sum of the libraries' payoffs and the profits of the publishers. Since the industry profit is just a transfer from libraries to publishers, social welfare is equal, up to a constant, to the total payoff the libraries obtain from consuming bundles of journals. Obviously, it is maximized when all libraries consume both bundles.

We consider a simultaneous pricing game among publishers. In the absence of the consortium, each publisher \( j \) simultaneously chooses \( P^i_j > 0 \) for \( i = 1, \ldots, n \), and then each library decides the bundle(s) to buy. Note that in this case, the market for each library can be studied in isolation. If instead the libraries have built a consortium, then each publisher \( j \) simultaneously chooses \( P^C_j > 0 \) and, after that, the consortium makes purchases. Notice that we require \( P^i_j > 0 \), and exclude \( P^i_j = 0 \), because in some cases a publisher \( j \) earns a library’s entire budget, and thus there is no money left for publisher \( j' \neq j \). Then our assumption of positive prices rules out the possibility that publisher \( j' \) gives away \( B_{j'} \) for free. Thus, in a sense we suppose that each publisher prefers not selling its bundle to selling it at zero price, which can be justified if there is an epsilon cost of contracting or billing.

### 2.2 Competition in the market for a given library

Consider competition in the market for a given library \( i (= 1, \ldots, n, C) \). In this subsection, we eliminate the superscript \( i \) and without loss of generality we assume \( U_A \geq U_B \). Then, from our previous papers, we have\(^{10}\)

\(^{10}\)In fact, in Jeon and Menicucci (2006, 2011) we assume that publishers play a sequential game in which first each publisher decides whether to be active or not, and then only active publishers compete in prices (libraries cannot buy from inactive publishers). However, when there are only two publishers, this sequential game yields the same outcome that is described by Lemma 1 for a simultaneous move game.
Lemma 1 (Jeon and Menicucci, 2006 and 2011) Consider competition between the two publishers in the market for a given library:

(i) if $M \leq U_A - U_B$, then publisher A charges $P_A = M$, publisher B charges an arbitrary $P_B > 0$, and the library buys only $B_A$;

(ii) if $U_A - U_B < M < U_A + U_B$, then publishers charge $P_A = \frac{1}{2}(M + U_A - U_B)$,
     $P_B = \frac{1}{2}(M + U_B - U_A)$, and the library buys both bundles;

(iii) if $U_A + U_B \leq M$, then publishers charge $P_A = U_A$, $P_B = U_B$, and the library buys both bundles.

When $M \leq U_A - U_B$, only publisher A succeeds in selling its bundle because even when A charges $P_A = M$ (the highest feasible price) the library’s payoff from buying only $B_A$, $U_A - M$, is larger than the payoff from buying only $B_B$, $U_B - P_B$, for any $P_B > 0$. On the other hand, if $M > U_A - U_B$ then the library buys both bundles and it is simple to see that $P_A = U_A$, $P_B = U_B$ when $M \geq U_A + U_B$. When instead $U_A - U_B < M < U_A + U_B$, prices are determined by the indifference condition

$$U_A - P_A = U_B - P_B \quad (1)$$

and the binding budget constraint

$$P_A + P_B = M. \quad (2)$$

In particular, (1) implies that the library is indifferent between purchasing only $B_A$ and purchasing only $B_B$. Thus no publisher $j$ ($j = A, B$) has an incentive to increase its price above $P_j$ since then the library can not afford to buy both bundles (because of the binding budget constraint) and would buy only the bundle of the rival publisher.

Lemma 1 applies both to each library without the consortium and also to the consortium. In the next sections, we compare the outcome without the consortium and the outcome with the consortium.

3 Consortium of $n$ libraries

In this section, we consider the model of $n$ libraries introduced in Section 2. We assume

A1: $M^i \leq U^i_A + U^i_B$ for $i = 1, ..., n$.

If Assumption A1 is not satisfied for library $i$, there is no competition between the two publishers in the market for library $i$ since each extracts the full surplus. Hence, this assumption implies that the two publishers face competition generated by the budget
constraint in the market for any given library \(i = 1, \ldots, n\). As a consequence, every library \(i\) ends up spending its whole budget to purchase the journals of the two publishers. Furthermore, in Section 5 in which we make the budget choice endogenous, \(A1\) is always satisfied. \(A1\) also implies that \(MC \leq UA + UB\), and thus also the consortium spends its whole budget to buy bundle(s). Therefore, in order to determine the effects of building a consortium on libraries’ payoffs, we only need to study how libraries’ consumption of bundles is affected.

Without loss of generality, we assume that \(\Delta C \equiv UA - UB\) is non-negative and that there exists an \(n'\) between 1 and \(n\) such that \(\Delta i \equiv Ui - UB \geq 0\) for \(i = 1, \ldots, n'\) and \(\Delta i < 0\) for \(i = n' + 1, \ldots, n\). Libraries \(1, \ldots, n'\) are called type A libraries (there is a non-empty set of type A libraries since \(UA \geq UB\)); the other libraries (if any) are called type B libraries.

Lemma 1 makes clear that the only characteristics of library \(i\) which matter are \(\Delta i\) and \(MC\). Without the consortium, library \(i\) of type \(j\) buys only \(Bj\) if \(MC > |\Delta i|\), buys both bundles if \(MC > |\Delta i|\), for \(j = A, B\). Likewise, the consortium buys only \(BA\) if \(MC > 0\), buys both bundles if \(MC > \Delta C\). These remarks deliver the following results.

**Proposition 1 (exogenous budget)** Suppose that the \(n(\geq 2)\) libraries form a consortium. Assume \(A1\) and suppose \(\Delta C \equiv UA - UB \geq 0\) without loss of generality.

(i) When \(\Delta C < MC\), the consortium buys both bundles and hence the payoff of each library is weakly larger than without the consortium. The consortium strictly increases the total payoff of the libraries unless each library buys both bundles without the consortium.

(ii) When \(MC \leq \Delta C\), the consortium buys only \(BA\) and hence the payoff of each library is weakly smaller than without the consortium. The consortium strictly reduces the total payoff of the libraries unless each library buys only \(BA\) without the consortium.

It is simple to see why this proposition is true. Without the consortium, each library with type \(j\) either buys only \(Bj\) or both bundles. When the consortium is formed and \(MC \leq \Delta C\), each library consumes only \(BA\) and therefore (i) a type B library is worse off; (ii) a type A library is unaffected if it buys only \(BA\) without consortium, otherwise is worse off. On the other hand, when the consortium buys both bundles, each library enjoys maximal consumption and this increases the payoff of each library which does not buy both bundles without the consortium.

Proposition 1 implies that a key issue is whether or not the inequality \(\Delta C < MC\) holds. This condition is most easily satisfied when the preferences of libraries over bundles are quite heterogenous that in the consortium the intensity of the preferences of type A libraries for \(BA\) over \(BB\) are more or less counterbalanced by the intensity of the preferences of type B libraries for \(BB\) over \(BA\). The ideal case is such that \(\Delta^1 + \ldots + \Delta^{n'} = -(\Delta^{n'+1} + \ldots + \Delta^n)\), that is \(\Delta C = 0\), which makes \(\Delta C < MC\) hold for any level of
budget of the consortium. For instance, when \( n = 2 \) this occurs if \( \Delta^1 = -\Delta^2 \). If instead \( \Delta^1 + ... + \Delta^n \) is much larger than \(-(\Delta^{n+1} + ... + \Delta^n)\), then \( \Delta^C \) is much larger than zero and the consortium buys only \( B_A \) if its budget is small. Therefore, forming a consortium is more likely to be beneficial for libraries the more they are heterogeneous in terms of preferences for bundles.

4 Consortium of two libraries

In this section we analyze our model for the case of \( n = 2 \) in order to obtain more precise results by focusing on the correlation between the two libraries’ preferences. For this purpose, we assume \( M^1 = M^2 \equiv M \) and maintain assumption A1.

As in the previous section, we define \( U^i_A = U^i_B \) for \( i = 1; 2 \), and without loss of generality we assume \( \Delta^1 \geq \Delta^2 \geq 0 \) (with at least one strict inequality). In words, library 1 prefers \( B_A \) to \( B_B \). If also library 2 prefers \( B_A \), then library 1 prefers \( B_A \) more than library 2. If conversely library 2 prefers \( B_B \), then library 1 prefers \( B_A \) more than library 2 prefers \( B_B \).

In order to simplify notation, let \( \rho \equiv \Delta^2/\Delta^1 \in [-1, 1] \) and \( \Delta \equiv \Delta^1 \). Notice that \( \rho \) is a measure of the correlation between the two libraries’ preferences. With this notation we have

\[
U^1_A - U^1_B = \Delta, \quad U^2_A - U^2_B = \rho \Delta, \quad U^C_A - U^C_B = (1 + \rho)\Delta (\geq 0).
\]

From Lemma 1 and Proposition 1, in the absence of the consortium, library 1 buys both bundles if and only if \( M > \Delta \), library 2 buys both bundles if and only if \( M > |\rho|\Delta \), and the consortium buys both bundles if and only if \( M > (1 + \rho)\Delta/2 \). Hence, we have:

**Observation:** If every single library buys both bundles in the absence of the consortium (i.e., if \( M > \Delta \)), then the consortium buys both bundles.

From now on we restrict attention to the case of \( M \leq \Delta \) and therefore library 1 buys only \( B_A \) in the absence of the consortium. We can further simplify notation by considering a normalized budget \( M' \equiv M/\Delta \in (0, 1] \). Hence, in what follows, the model has only two parameters: \( M' \in (0, 1] \) and \( \rho \in [-1, 1] \). For instance, in the absence of the consortium, if \( \rho = 1 \) then both libraries buy only \( B_A \); if \( \rho = -1 \), library 1 buys only \( B_A \) and library 2 buys only \( B_B \); if \( \rho = 0 \), library 1 buys only \( B_A \) and library 2 buys both bundles. From these remarks and Proposition 1 we obtain next lemma.

**Lemma 2** Suppose that the two libraries form a consortium and that \( M' \equiv M/\Delta \leq 1 \). Assume A1. Then library 1 buys only \( B_A \) in the absence of the consortium and

(i) if \( M' > (1 + \rho)/2 \), the consortium buys both bundles, which strictly increases the libraries’ aggregate payoff.
Figure 1: $A^+(\rho)$, $A^-(\rho)$ and $A^0(\rho)$.

(ii) if $M' \leq (1 + \rho)/2$, the consortium buys only $B_A$. This reduces the libraries’ total payoff if $M' > \rho$, but it does not affect neither any library’s consumption nor its payoff if $M' \leq \rho$.

Figure 1 represents the sets of $(\rho, M')$ which satisfy the conditions in Lemma 2(i) and Lemma 2(ii). The region denoted by $+$ is such that $M' > (1 + \rho)/2$; the region denoted by $-$ is such that $\rho < M' \leq (1 + \rho)/2$; the region denoted by 0 is such that $M' \leq \rho < (1 + \rho)/2$. For each $\rho \in [-1, 1]$, let $L^+(\rho) \in [0, 1]$ represent the length of the set of values of $M'$ such that the consortium strictly increases the total payoff of the libraries. Similarly, let $L^-(\rho) \in [0, 1]$ (resp. $L^0(\rho) \in [0, 1]$) represents the length of the set of values of $M'$ such that the consortium strictly reduces the libraries’ total payoff (resp. does not affect the total payoff). Using Lemma 2 it is possible to compute each length, and thus we obtain:

**Proposition 2** (exogenous budget and correlation) Suppose that the two libraries form a consortium, and that $M' \leq 1$. Under Assumption A1:

(i) The length of the set of values of $M'$ such that the consortium strictly increases the libraries’ total payoff, $L^+(\rho)$, satisfies $L^+(-1) = 1$, $L^+(1) = 0$ and linearly decreases with $\rho$, that is $L^+(\rho)$ linearly shrinks as the degree of correlation increases.

(ii) The length of the set of values of $M'$ such that the consortium strictly reduces the libraries’ total payoff, $L^-(\rho)$, satisfies $L^-(0) = 1/2$, $L^-(1) = L^-(1) = 0$ and linearly
decreases with |μ|, that it $L^-(μ)$ linearly shrinks as the absolute degree of correlation increases.

**Corollary 1** Under Assumption A1:

(i) In the case of perfectly negative correlation, $μ = -1$, the consortium always strictly increases the libraries’ total payoff.

(ii) In the case of perfectly positive correlation, $μ = 1$, the consortium has no impact on the libraries’ total payoff.

In order to provide an intuition, let us first consider the extreme case of two identical libraries. Then, the consortium has no impact since the payment and the consumption of each library (and each publisher’s profit) are just like in the absence of the consortium. More generally, Lemma 2(ii) and Figure 1 show that the consortium has no impact as long as the degree of positive correlation is strong enough with respect to the budget, i.e. if $M' \leq μ$. Then, every library consumes only $B_A$ regardless of whether the two libraries form the consortium or not.

Let us now consider the other extreme case of perfectly negative correlation (i.e. $μ = -1$). Then, in the absence of the consortium, each library consumes only its preferred bundle: library 1 consumes only $B_A$ and library 2 consumes only $B_B$. On the contrary, after they form the consortium, the consortium buys both bundles. This occurs because the opposite preferences of the libraries make the market power of each publisher symmetric in the case of the consortium, and this creates a level-playing field for the two publishers (without affecting the profit of any publisher).

Now let us consider the middle case of no correlation (i.e. $μ = 0$). Then, in the absence of the consortium, library 1 consumes only $B_A$ and library 2 consumes both bundles. In this case, the consortium increases (resp. reduces) the libraries’ payoff if its budget is large enough, i.e. if $M' > 1/2$ (resp. small enough i.e. $1/2 \geq M'$). If the budget is small, publisher A can export its residual monopoly power from library 1 to library 2 in order to monopolize the market for the consortium (and increase its profit). On the contrary, if the budget is large enough, publisher A’s market power is not strong enough to monopolize the entire market of the consortium and therefore the consortium buys both bundles (but the profit of publisher A still increases).\(^1\)

Another way to see that a lower $μ$ makes it more likely that a consortium is beneficial consists in noticing that in order to buy both bundles, the consortium needs to have a budget larger than $(1+μ)Δ$, which is increasing in $μ$. Therefore, if for instance each library

\(^1\) As the analysis of the three cases $μ = -1, μ = 0, μ = 1$ suggests, under the consortium the profit of A (the profit of B) is weakly higher (weakly smaller) than without the consortium, for any $M' \leq 1$ and any $μ \in [-1, 1]$, because the consortium allows A to export its residual monopoly power from library 1 to library 2.
buys only one bundle without consortium and the libraries form a consortium aimed at buying both bundles, the required budget for the consortium is smaller the smaller is \( \rho \) in \([-1, 1]\).

5 Endogenous budget

Up to now, we assumed that each library’s budget is given. In this section, we continue to analyze the case of two libraries but relax this assumption. Instead, we assume that a public authority perfectly internalizing each library’s payoff determines each library’s budget before publishers choose prices. For instance, a state authority determines the budget of the libraries of the state’s public universities. The timing of the game we consider is as follows:

- Stage 1: A public authority determines the budget for each library \( i \) (or the budget for the consortium).
- Stage 2: Each publisher simultaneously chooses a personalized price for its bundle of journals to each library (or the consortium).
- Stage 3: Each library \( i \) (or the consortium) decides which bundle(s) to buy.

Consider the market for library \( i \) for instance. According to Lemma 1, any positive \( M^i \) smaller than \( U^i_A - U^i_B \) allows the library to consume \( B_A \) and any \( M^i \) higher than \( U^i_A - U^i_B \) allows the library to consume both bundles. The library’s payoff is \( U^i_A - M^i \) in the first case and \( U^i_A + U^i_B - M^i \) in the second case. Since the authority wants to minimize the payment to publishers given the consumption of the library, the Supremum of the library’s payoff when its budget is endogenous is given by \( U^i_A \) in the first case and \( 2U^i_B \) in the second case. Therefore, we have:

**Lemma 3** Consider competition between two publishers in the market for a given library (or for the consortium) when its budget is endogenously chosen by an authority who perfectly internalizes the library’s payoff. Assume \( U_A \geq U_B \) without loss of generality. Then, the Supremum of the library’s payoff is \( \max\{U_A, 2U_B\} \).

In the equilibrium without consortium, each library consumes only its preferred bundle or both bundles. Let \((M,D)^1\),\(^12\) for instance, represent the situation in which library 1 consumes only one bundle (i.e. \( B_A \)) and library 2 consumes both bundles in the equilibrium without consortium; \((M,M)\), \((D,M)\) and \((D,D)\) are similarly defined. As in the

\(^{12}\)M refers to monopoly and D refers to duopoly.
previous section, we define $\Delta \equiv U^1_A - U^1_B > 0$, $\rho \equiv \frac{U^2_A - U^2_B}{\Delta}$, and without loss of generality we assume that $\rho \in [-1,1]$.

In next lemma we consider the case of $\rho \geq 0$ (positive correlation). We have:

**Lemma 4** (positive correlation) Consider competition between two publishers under endogenous budget. Consider $\rho > 0$.

(i) In the case of $(M,M)$ or $(D,D)$, building a consortium has no effect on the bundle(s) consumed and on the payoffs of the libraries.

(ii) In the case of $(M,D)$ or $(D,M)$, building a consortium affects the bundle(s) consumed and strictly reduces the total payoffs of the libraries.

Consider first the case of $(M,M)$, which is such that $U^i_A \geq 2U^i_B$ holds for $i = 1, 2$, and therefore $U^C_A \geq 2U^C_B$. As a consequence, the authority induces the consortium to consume only $B_A$; thus building a consortium has no effect on the bundle consumed and on the libraries’ payoffs. The same logic applies to the case of $(D,D)$, since then $U^i_A \leq 2U^i_B$ holds for $i = 1, 2$ and $U^C_A \leq 2U^C_B$.

Consider now for instance the case of $(M,D)$. Note first that the authority cannot achieve this pattern of consumption through a consortium since under a consortium, both libraries consume either the single bundle $B_A$ or both bundles. Moreover, given $B_A$ or $(B_A, B_B)$ that the consortium consumes in equilibrium, the authority can achieve the same consumption pattern without the consortium at the same total price. This implies that under the consortium the authority chooses between the alternatives $(M,M)$ and $(D,D)$, a subset of the alternatives available without the consortium. Since the authority chooses $(M,D)$ in the absence of the consortium, a revealed preference argument implies that $(M,D)$ gives a higher payoff than $(M,M)$ or $(D,D)$. Therefore building a consortium reduces the total payoffs of the libraries.

Now we consider the case of $\rho < 0$ (negative correlation), but in order to reduce the number of cases, we assume that both libraries obtain the same total utility from consuming both bundles:

**A2**: $(U^1_A + U^1_B) / 2 = (U^2_A + U^2_B) / 2 \equiv U$.

In the assumption, $U$ represents the average utility from both bundles. Hence, we have

\[
\begin{align*}
(U^1_A, U^1_B) &= (U + \Delta/2, U - \Delta/2), \\
(U^2_A, U^2_B) &= (U - |\rho| \Delta/2, U + |\rho| \Delta/2), \\
(U^C_A, U^C_B) &= (2U + (1 - |\rho|)\Delta/2, 2U - (1 - |\rho|)\Delta/2).
\end{align*}
\]
Then, we can normalize the utilities by dividing them by $\Delta$. Let $U' \equiv U/\Delta$, which must be larger than $1/2$ since $U_B' > 0$. Let $U_i' = U_i'/\Delta$ for $i = 1, 2, C$ and $j = A, B$. Hence

$$
\begin{align*}
(U_A', U_B') &= (U' + 1/2, U' - 1/2), \\
(U_A^{2'}, U_B^{2'}) &= (U' - |\rho|/2, U' + |\rho|/2), \\
(U_C', U_B') &= (2U' + (1 - |\rho|)/2, 2U' - (1 - |\rho|)/2).
\end{align*}
$$

Given this normalization, we have only two parameters: $U' > 1/2$ and $\rho \in [-1, 0)$. We have:

**Lemma 5 (negative correlation)** Consider competition between the two publishers under endogenous budget with $\rho < 0$. Assume A2.

(i) For any $\rho < 0$, in the absence of the consortium, $(D,D)$ arises if and only if $U' \geq 3/2$. Then, under the consortium, the libraries consume both bundles and the consortium strictly increases the total payoffs of the libraries.

(ii) Consider $3/2 > U' > 1/2$.

(a) For $-1/3 \leq \rho < 0$: In the absence of the consortium, only $(M,D)$ arises. Under the consortium, the libraries consume both bundles if and only if $U' \geq 3(1 - |\rho|)/4$. The consortium strictly increases the total payoffs of the libraries if and only if $U' > (3 - 4|\rho|)/2$.

(b) For $-1 \leq \rho < -1/3$: In the absence of the consortium, $(M,D)$ arises if $U' > 3|\rho|/2$ and $(M,M)$ arises otherwise. Under the consortium, the libraries always consume both bundles. The consortium strictly increases the total payoffs of the libraries if and only if $U' > \frac{1}{2}$ $\max\{3 - 4|\rho|, \frac{3 - |\rho|}{2}\}$.

This lemma reveals first that, for any $\rho < 0$, whenever the average value of the bundles is large enough (i.e. $U' \geq 3/2$) such that $(D,D)$ arises without consortium, then the consortium strictly increases the total payoffs of the libraries. This is because building the consortium does not affect consumption but reduces the gap between the willingness to pay for bundle of $A$ and the one for bundle of $B$; this in turn increases competition between the two publishers and allows the libraries to consume both bundles at a lower total price. Precisely, without the consortium, the total price paid is $1 + |\rho|$ but the consortium pays only $1 - |\rho|$.

When the average value of the bundles is not large (i.e. $3/2 > U' > 1/2$), either $(M,D)$ or $(M,M)$ occurs without consortium. To sharpen the intuition, let us consider the two extreme cases of perfect negative correlation and no correlation. In the extreme case of perfect negative correlation, building a consortium always strictly increases the total payoffs of the libraries. In this case, only $(M,M)$ arises in the absence of the consortium: library 1 consumers only the bundle of $A$ and library 2 consumes only the bundle of $B$. Then, building a consortium creates a level playing field between the two publishers.
such that the consortium can consume both bundles at almost zero price. In contrast, in the extreme case of no correlation, only (M,D) occurs without consortium. Then, for the revealed preference argument explained right after Lemma 4, building a consortium always strictly reduces the total payoffs of the libraries. For the general case of negative correlation (i.e. $0 > \rho > -1$), there exists a cut-off value of $U' \equiv U/\Delta$ above which building a consortium strictly increases the sum of the libraries’ payoffs. This cut-off strictly decreases with the degree of the negative correlation $|\rho|$.

Figure 2 describes the consumption patterns in the absence of the consortium under A2. Figure 3 shows the region (marked with +) under which building the consortium strictly increases the sum of the libraries’ payoffs, the region (marked with 0) under which building the consortium does not affect it and the region (marked with -) under which building the consortium strictly reduces it. Summarizing, we have:

**Proposition 3 (endogenous budget and correlation)** Consider competition between two publishers under endogenous budget.

(i) When the two libraries’ preferences are positively correlated (i.e. $\rho \geq 0$), building a consortium either has no effect on the sum of the libraries’ payoffs or strictly reduces
it. Under the assumption A2, the range of $U'$ for which the consortium is harmful shrinks with the degree of correlation such that it disappears for the prefect positive correlation.

(ii) When the two libraries’ preferences are negatively correlated (i.e. $\rho < 0$), under the assumption A2, there exists a cut-off value of $U' \equiv U/\Delta$ above which building a consortium strictly increases the sum of the libraries’ payoffs. This cut-off strictly decreases with the degree of the correlation $|\rho|$ and reaches $1/2$ for perfect negative correlation.

**Corollary 2** Under the assumption A2;

(i) In the case of perfectly negative correlation, $\rho = -1$, the consortium always strictly increases the libraries’ total payoff.

(ii) In the case of perfectly positive correlation, $\rho = 1$, the consortium has no impact on the libraries’ total payoff.

When we compare Figure 1 of exogenous budget and Figure 3 of endogenous budget, it is remarkable that they share a number of features even if the parameter represented by the vertical axis is different in the two figures. First, Corollary 1 and Corollary 2 have the identical predictions for the two extreme cases of perfect positive and perfect negative correlation. Second, given negative correlation, the parameter range for which consortium is beneficial increases with the absolute degree of correlation both in Proposition 2(i)
and Proposition 3(ii). Third, given positive correlation, the parameter range for which consortium is harmful decreases with the degree of correlation both in Proposition 2(ii) and Proposition 3(i). The key differences arise for the case of positive correlation: while building a consortium can be strictly beneficial for certain parameter range when the budget is exogenously given, it can never be strictly beneficial in the case of endogenous budget.

6 Policy implications

Our results generate the following implications for the long term strategy to build a library consortium. First, libraries with similar preferences are likely to lose from building a consortium. Therefore, it is not desirable to build a consortium around them as long as building it requires extra effort and resources.

Second, libraries with opposite preferences almost always gain from building a consortium. In case of a large number of libraries, if their preferences are heterogenous enough that no single publisher can exercise a strong market power, this would maximize the consumption set of the consortium (and hence of each member library). More generally, libraries should use the consortium as an opportunity to create a level-playing field among powerful publishers. In the case of a consortium based on a geographic area, if the libraries within the area have preferences heterogenous enough, it is desirable to build the consortium.

Last, our results also point out a strong tension between a short-term strategy and a long-term strategy as long as the former dictates forming a consortium with libraries with homogenous preferences to benefit from quantity discounts. Then, the strategy of maximizing the short-run benefit is likely to deliver a negative benefit in the long run after publishers adjust their tariffs to extract surplus and the funding authority reacts to the new tariffs by adjusting the budget.

References


